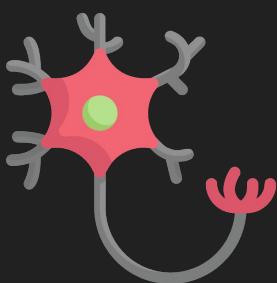
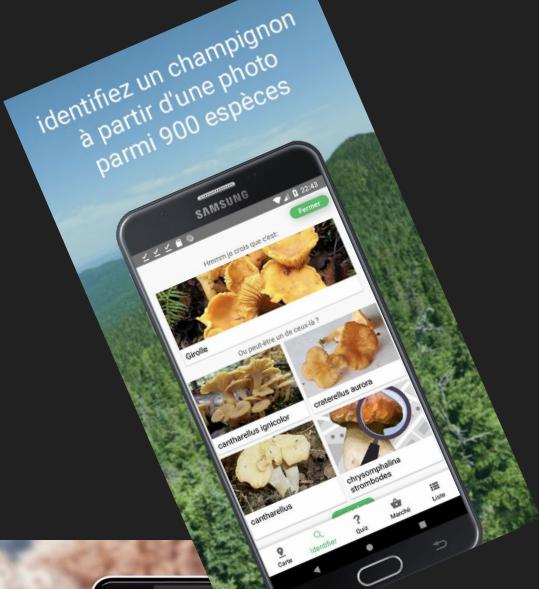
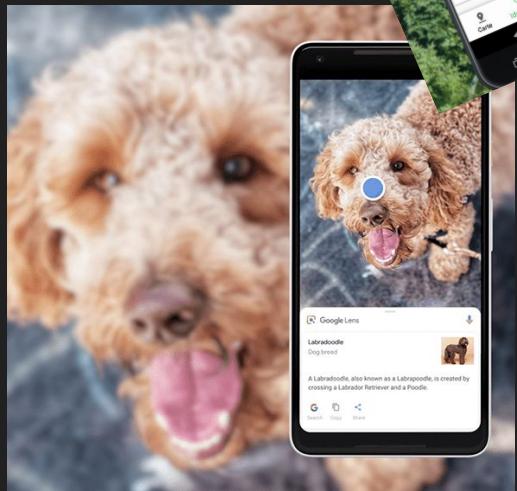
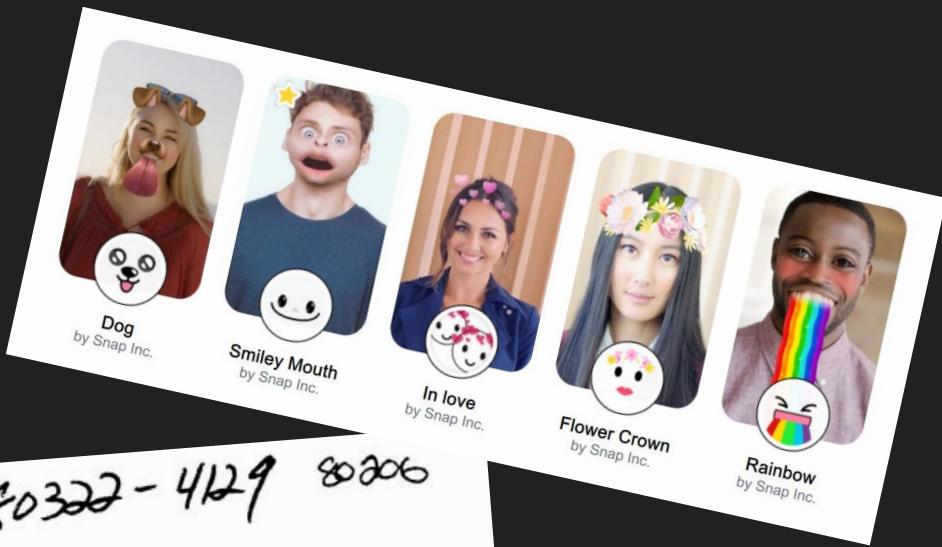


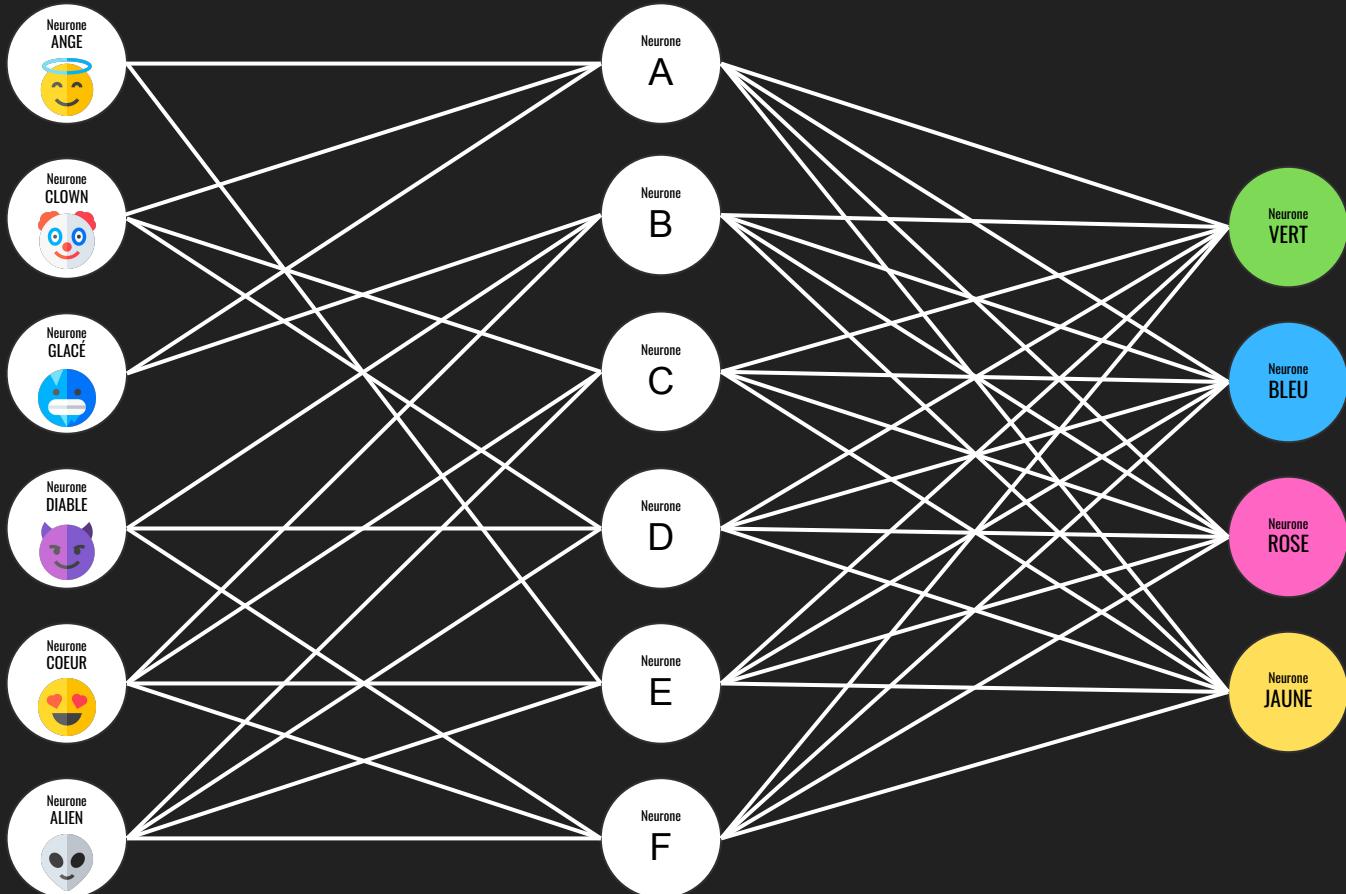
# Connecte tes neurones !

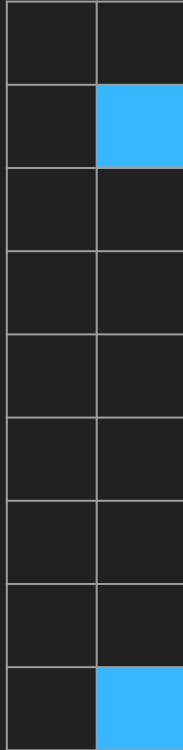




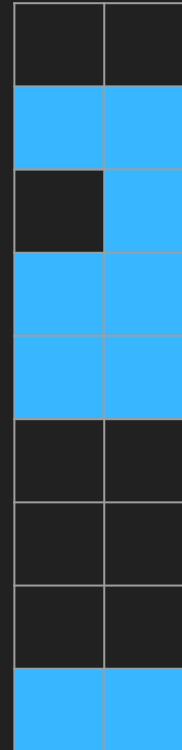
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35460 44209



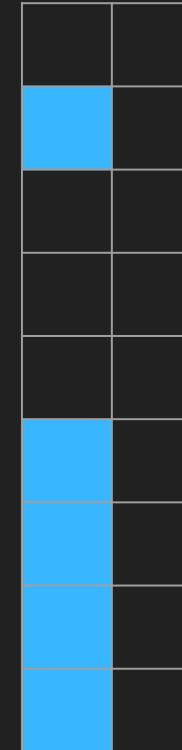




Neurone

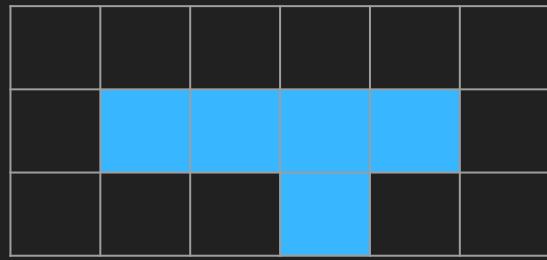


Neurone

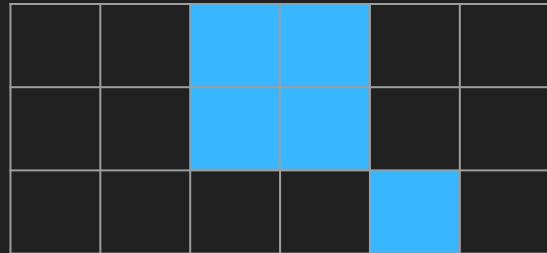


Neurone

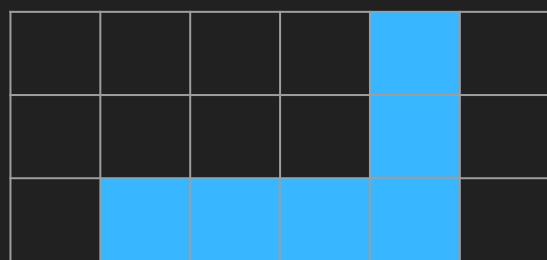
Neurone

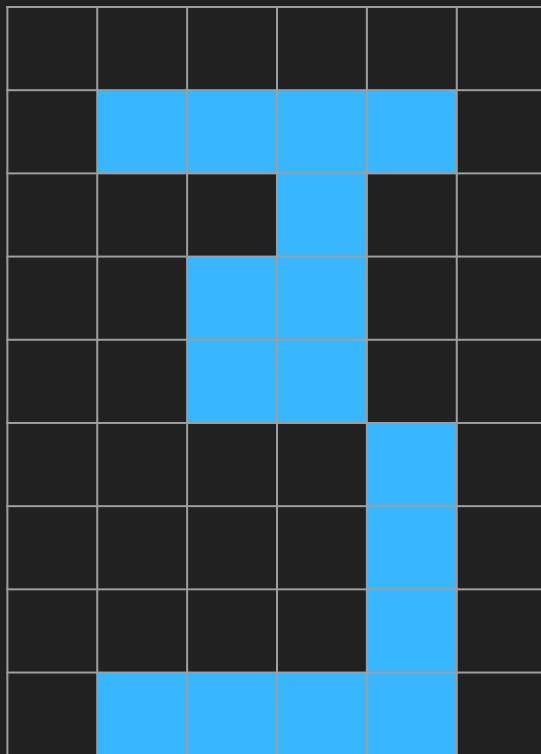


Neurone

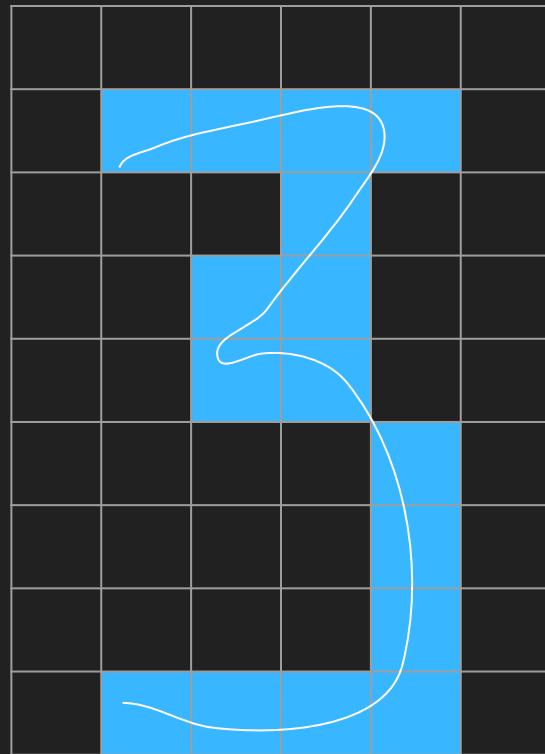


Neurone

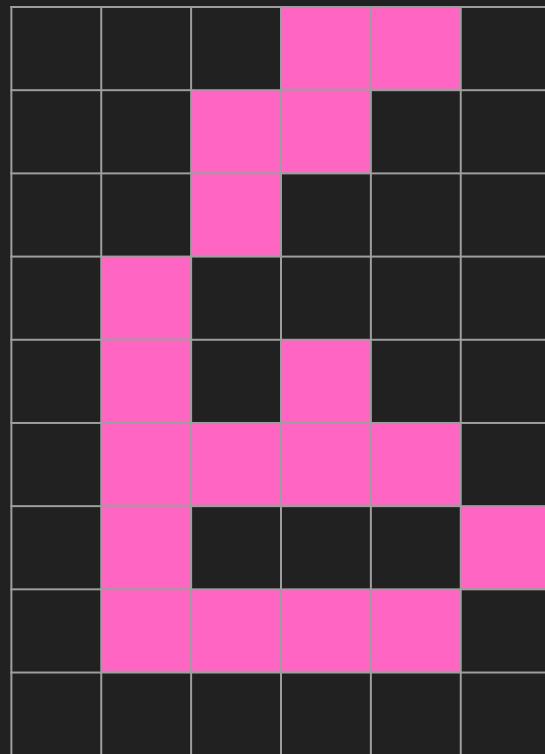














## Rôle du neurone F

1 FAIS LE CALCUL SUIVANT :

$$\text{🐱} + \text{👽} - \text{😍} = ?$$

2 TROUVE LA RÉPONSE À MONTRER :

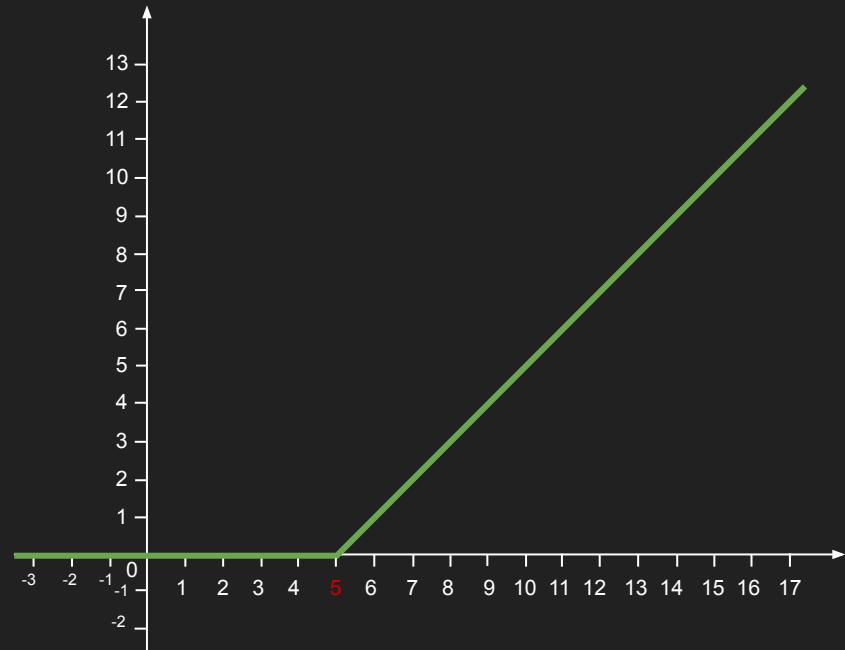
Résultat du calcul



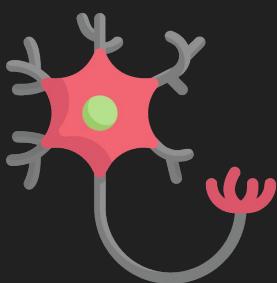
1 2 3 4 5 6 7 8 9

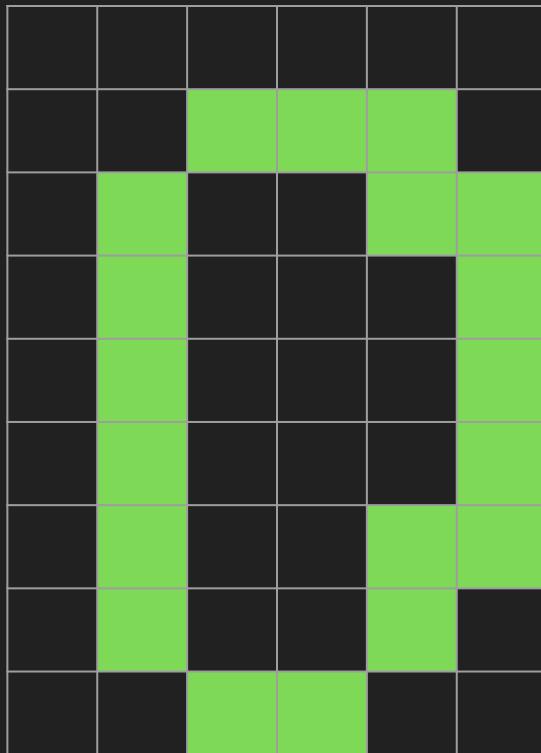
Réponse  
à montrer

0 0 0 0 0 1 2 3 4



# Connecte tes neurones !





Résultat du calcul

Sortie du  
neurone

---

Neurone A

---

Neurone B

---

Neurone C

---

Neurone D

---

Neurone E

---

Neurone F

	Résultat du calcul	Sortie du neurone
Neurone A	7	0
Neurone B		
Neurone C		
Neurone D		
Neurone E		
Neurone F		

	Résultat du calcul	Sortie du neurone
Neurone A	7	0
Neurone B	3	0
Neurone C		
Neurone D		
Neurone E		
Neurone F		

	Résultat du calcul	Sortie du neurone
Neurone A	7	0
Neurone B	3	0
Neurone C	21	4
Neurone D		
Neurone E		
Neurone F		

	Résultat du calcul	Sortie du neurone
Neurone A	7	0
Neurone B	3	0
Neurone C	21	4
Neurone D	5	0
Neurone E		
Neurone F		

	Résultat du calcul	Sortie du neurone
Neurone A	7	0
Neurone B	3	0
Neurone C	21	4
Neurone D	5	0
Neurone E	19	3
Neurone F		

	Résultat du calcul	Sortie du neurone
Neurone A	7	0
Neurone B	3	0
Neurone C	21	4
Neurone D	5	0
Neurone E	19	3
Neurone F	7	2

	Résultat du calcul	Sortie du neurone
Neurone A	7	0
Neurone B	3	0
Neurone C	21	4
Neurone D	5	0
Neurone E	19	3
Neurone F	7	2

ENVOYÉ À LA COUCHE SUIVANTE

Résultat du calcul

Sortie du neurone

---

Neurone vert

---

Neurone bleu

---

Neurone rose

---

Neurone jaune

Résultat du calcul

Sortie du neurone

---

Neurone vert

9

3

---

Neurone bleu

---

Neurone rose

---

Neurone jaune

## Résultat du calcul

## Sortie du neurone

Neurone vert	9	3
Neurone bleu	- 7	0
Neurone rose		
Neurone jaune		

Résultat du calcul      Sortie du neurone

Neurone vert	9	3
Neurone bleu	- 7	0
Neurone rose	-3	0
Neurone jaune		

Résultat du calcul      Sortie du neurone

Neurone vert	9	3
Neurone bleu	- 7	0
Neurone rose	-3	0
Neurone jaune	1	0

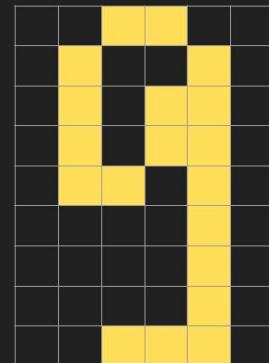
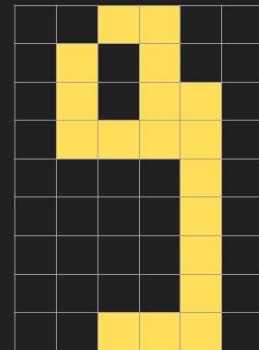
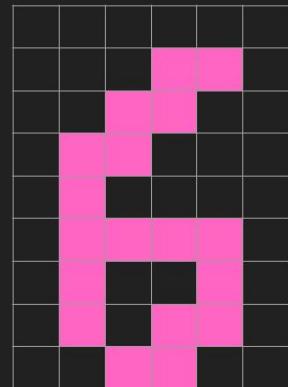
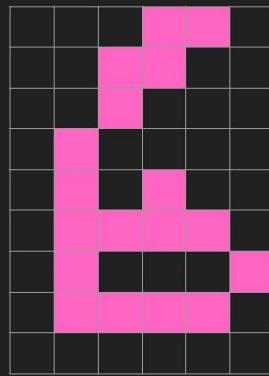
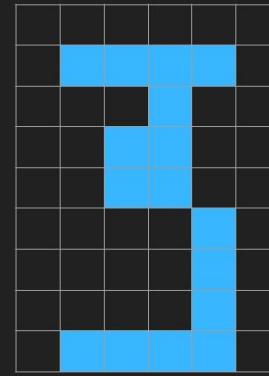
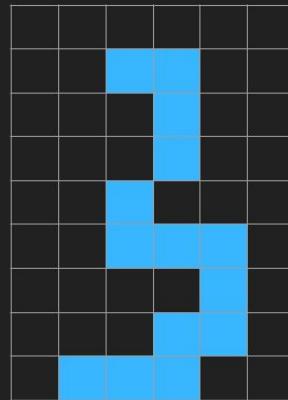
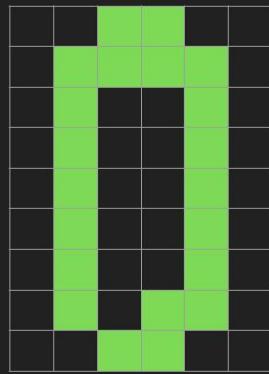
Résultat du calcul

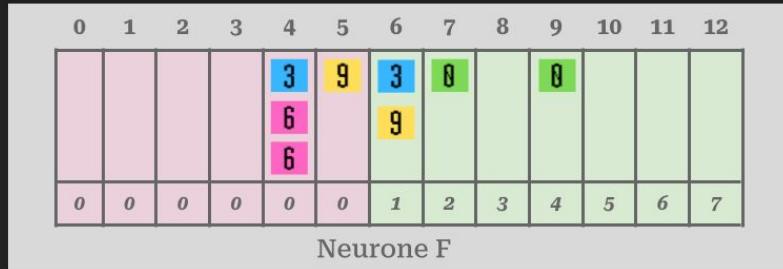
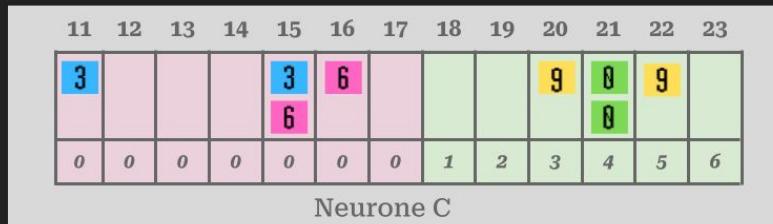
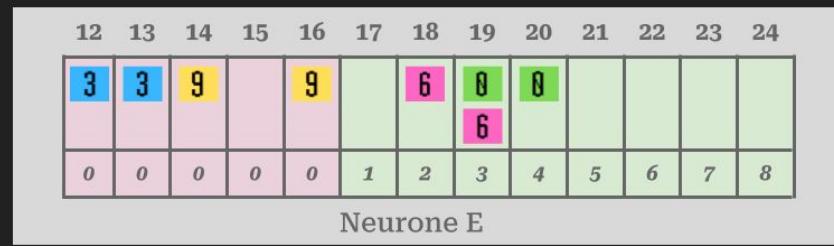
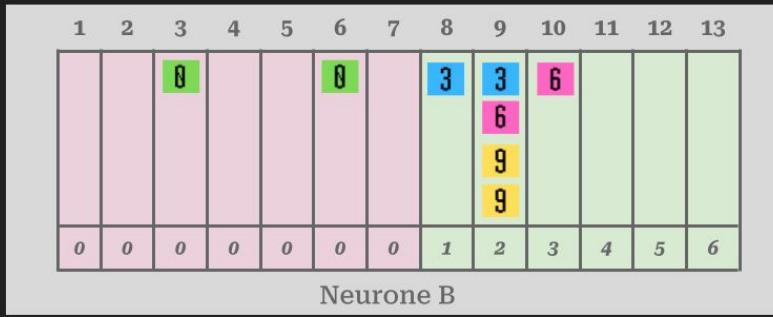
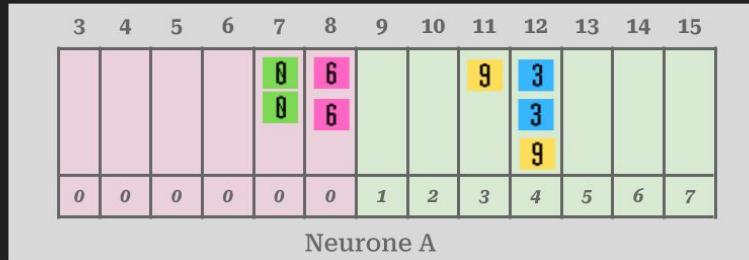
Sortie du neurone

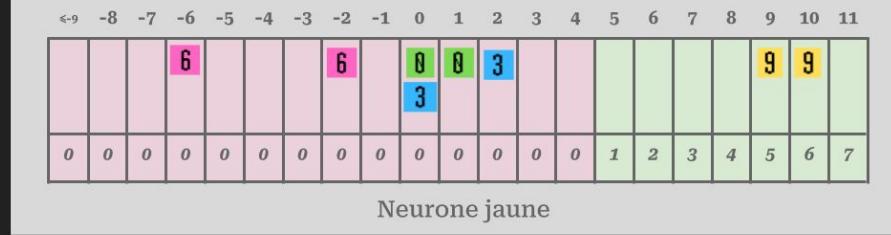
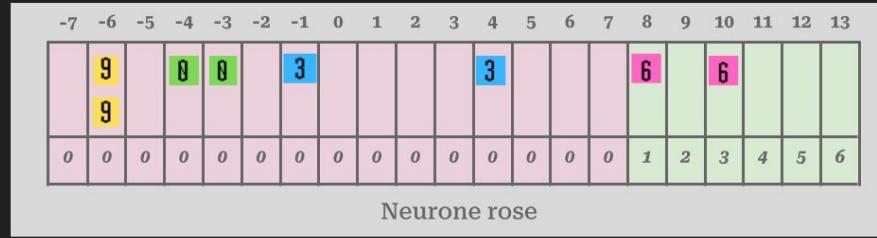
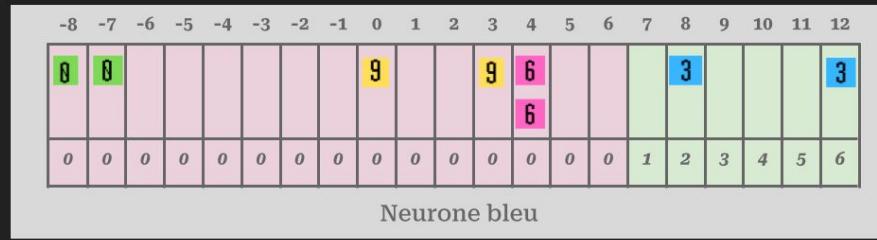
Neurone vert	9	3
Neurone bleu	- 7	0
Neurone rose	-3	0
Neurone jaune	1	0

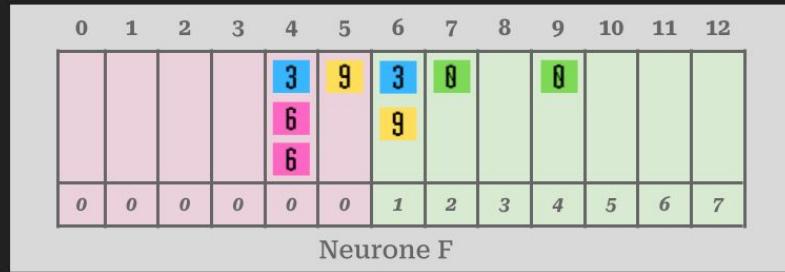
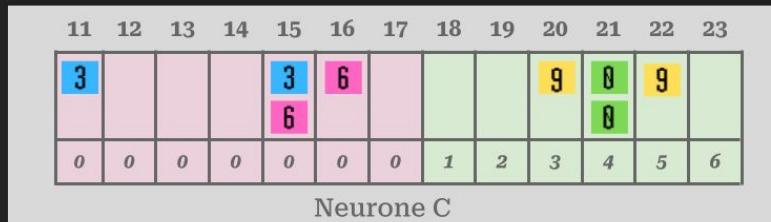
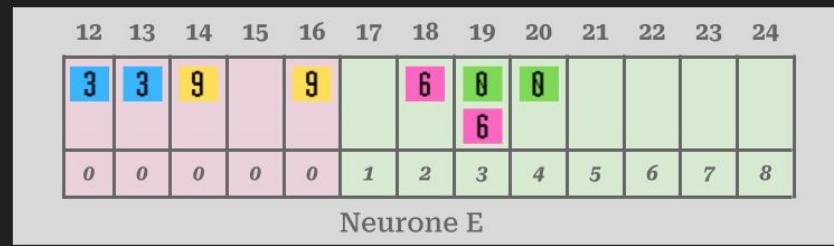
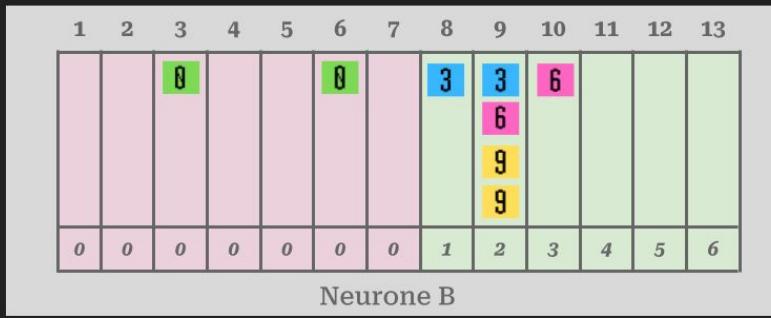
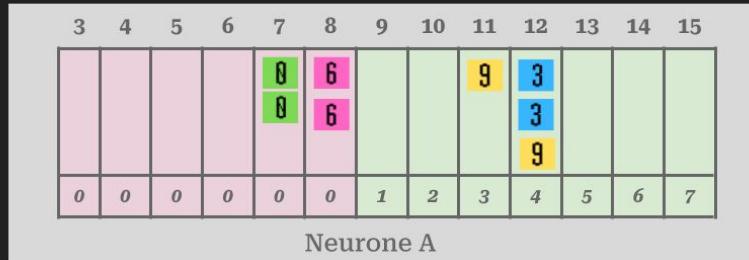
C'EST UN 0 !



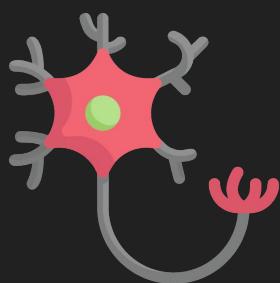


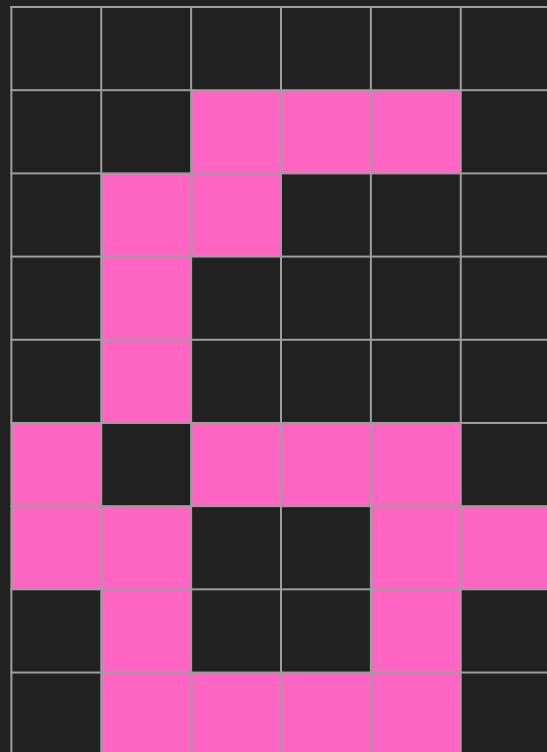






# Connecte tes neurones !





3	4	5	6	7	8	9	10	11	12	13	14	15
0	0	0	0	0	0	1	2	3	4	5	6	7
0	0	0	0	0	0	0	0	0	0	0	0	0

Neurone A

3	4	5	6	7	8	9	10	11	12	13	14	15
0	0	0	0	0	1	2	3	4	5	6	7	8
0	0	0	0	0	0	0	0	0	0	0	0	0

Neurone D

1	2	3	4	5	6	7	8	9	10	11	12	13
0	0	0	0	0	0	0	1	2	3	4	5	6
0	0	0	0	0	0	0	0	0	0	0	0	0

Neurone B

12	13	14	15	16	17	18	19	20	21	22	23	24
0	0	0	0	0	1	2	3	4	5	6	7	8
0	0	0	0	0	0	0	0	0	0	0	0	0

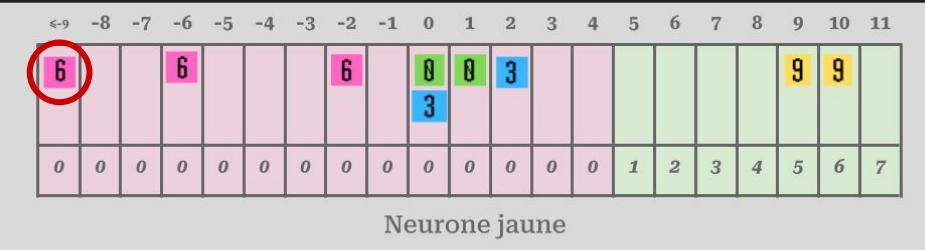
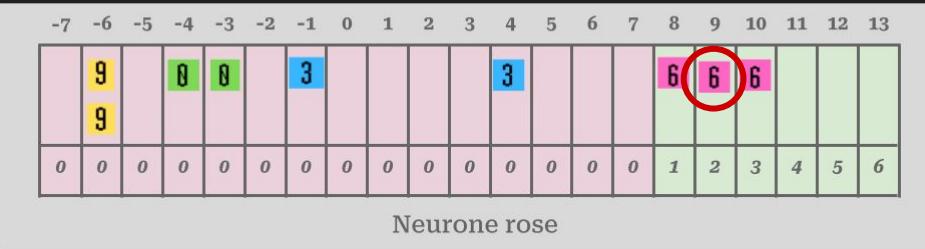
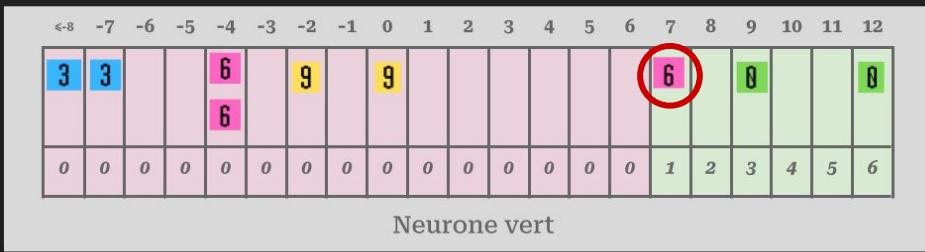
Neurone E

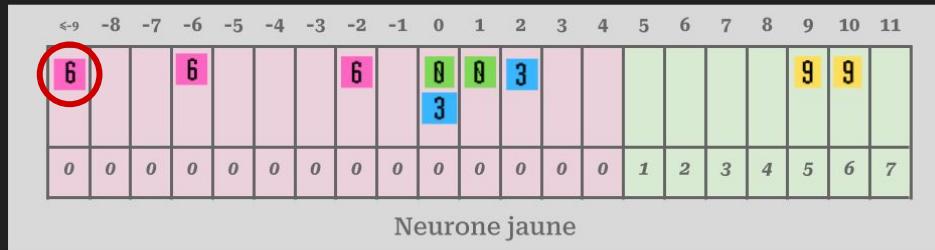
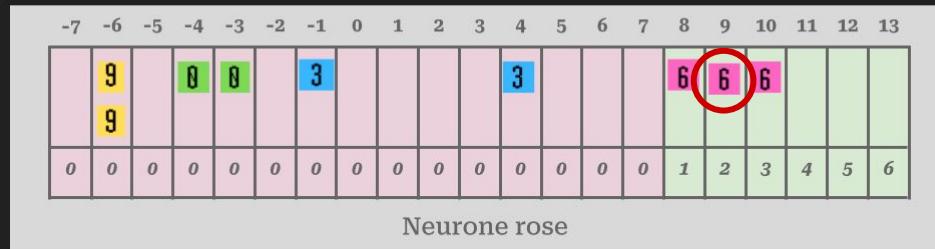
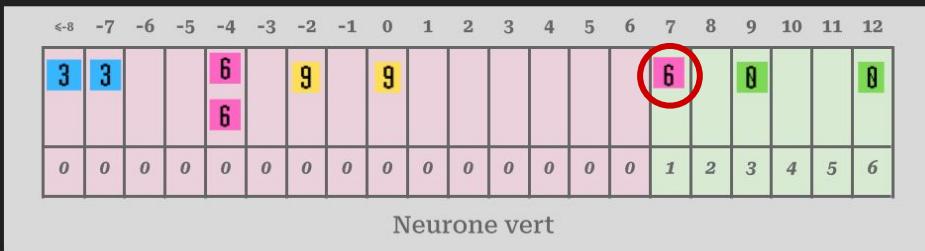
11	12	13	14	15	16	17	18	19	20	21	22	23
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0	0	0	0	0	0	0	0	0	0	0	0	0

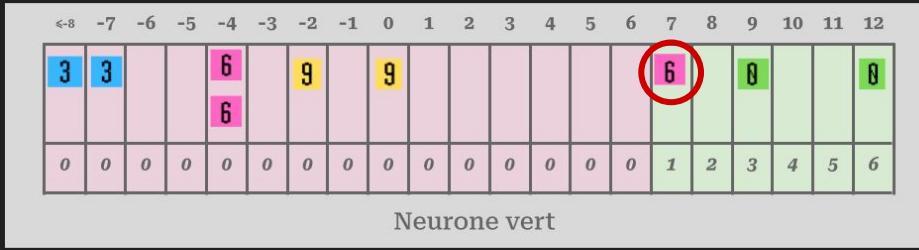
Neurone C

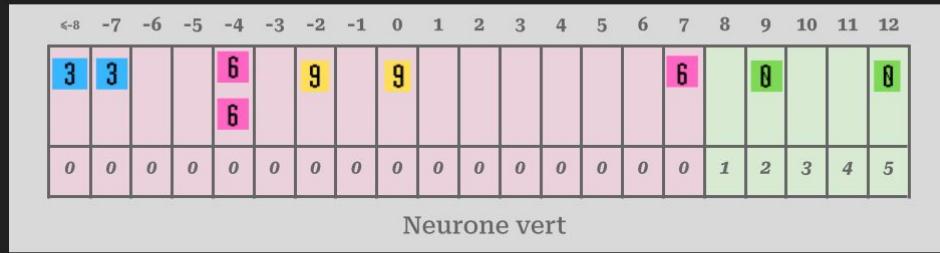
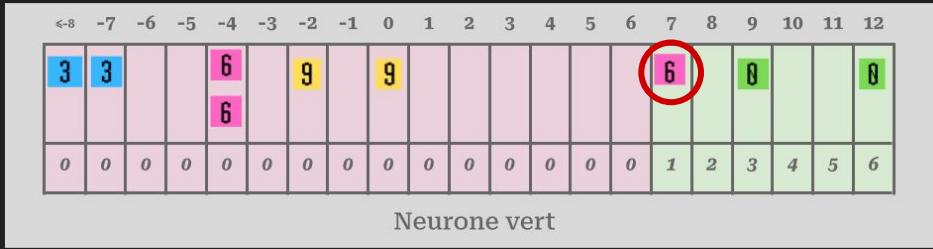
0	1	2	3	4	5	6	7	8	9	10	11	12
0	0	0	0	0	1	2	3	4	5	6	7	8
0	0	0	0	0	0	0	0	0	0	0	0	0

Neurone F









<-8	-7	-6	-5	-4	-3	-2	-1	0	1	2	3	4	5	6	7	8	9	10	11	12
3	3				6			9	9						6		8		8	
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	2	3	4	5



Neurone vert

-8	-7	-6	-5	-4	-3	-2	-1	0	1	2	3	4	5	6	7	8	9	10	11	12
0	0				6			9			9	6				3			3	
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	2	3	4	5



Neurone bleu

-7	-6	-5	-4	-3	-2	-1	0	1	2	3	4	5	6	7	8	9	10	11	12	13
9			0	0		3					3				6	6	6			
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	2	3	4	5



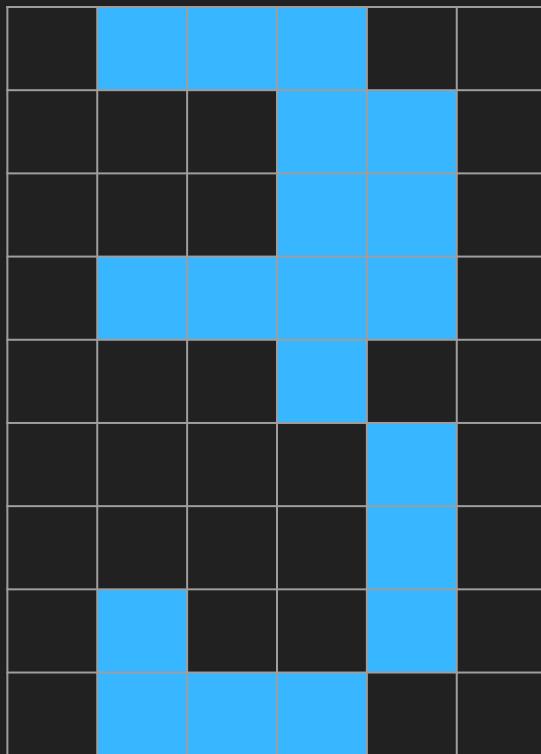
Neurone rose

<-9	-8	-7	-6	-5	-4	-3	-2	-1	0	1	2	3	4	5	6	7	8	9	10	11
6			6				6		0	0	3					9	9			
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	2	3	4	5



Neurone jaune





3	4	5	6	7	8	9	10	11	12	13	14	15
0	0	0	0	0	0	1	2	3	4	5	6	7
0	0	0	0	0	0	0	0	3	3	0	0	0

Neurone A

3	4	5	6	7	8	9	10	11	12	13	14	15
0	0	0	0	0	1	2	3	4	5	6	7	8
0	0	0	0	0	0	0	0	0	3	3	6	6

Neurone D

1	2	3	4	5	6	7	8	9	10	11	12	13
0	0	0	0	0	0	0	1	2	3	4	5	6
0	0	0	0	0	0	0	0	0	3	6	0	0

Neurone B

12	13	14	15	16	17	18	19	20	21	22	23	24
0	0	0	0	0	1	2	3	4	5	6	7	8
0	0	0	0	0	0	0	0	0	0	3	3	6

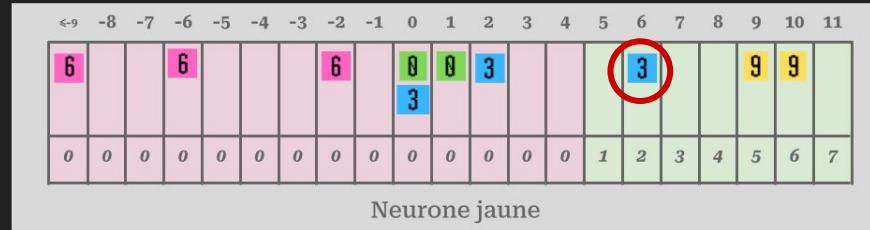
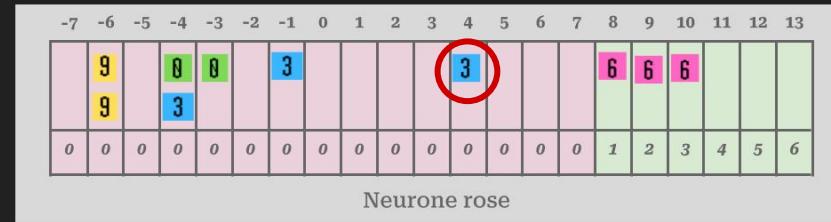
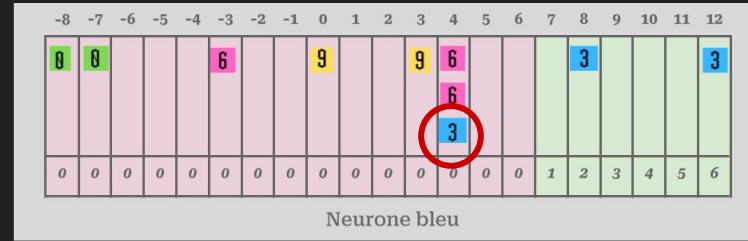
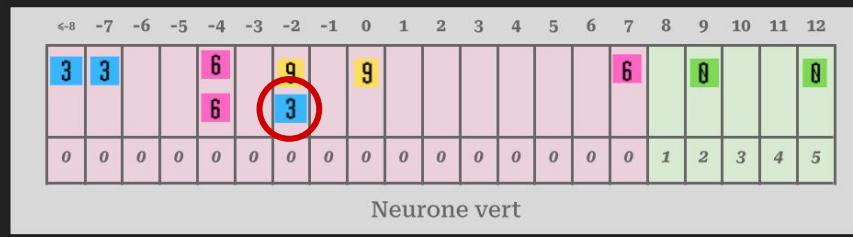
Neurone E

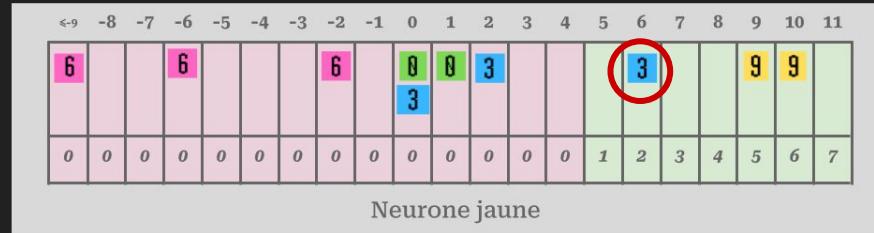
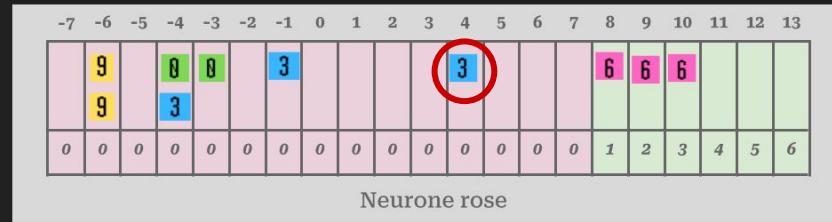
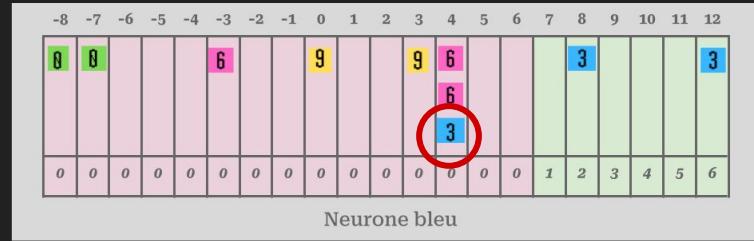
11	12	13	14	15	16	17	18	19	20	21	22	23
0	0	0	0	0	0	0	0	3	9	0	0	0
0	0	0	0	0	0	0	0	6	6	0	0	0

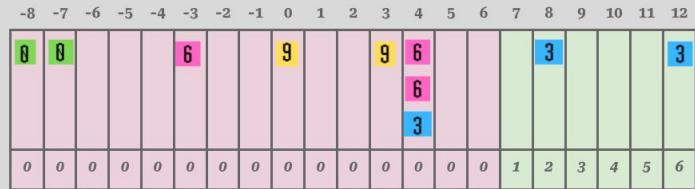
Neurone C

0	1	2	3	4	5	6	7	8	9	10	11	12
0	0	0	0	0	0	1	2	3	3	9	0	0
0	0	0	0	0	0	0	0	6	6	0	0	0

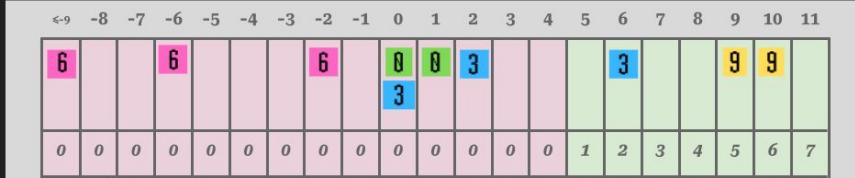
Neurone F



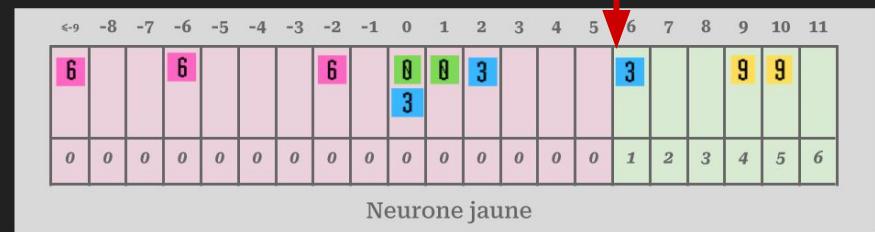
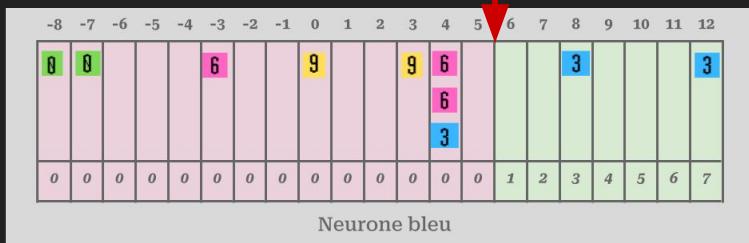
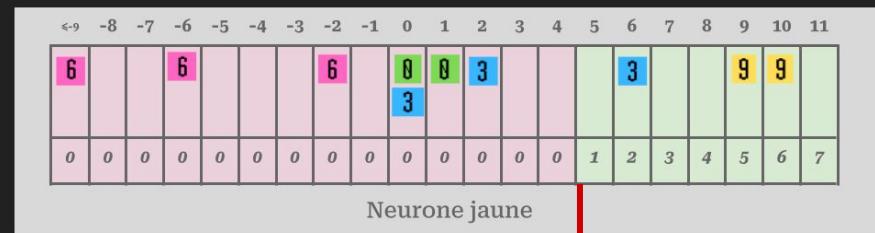
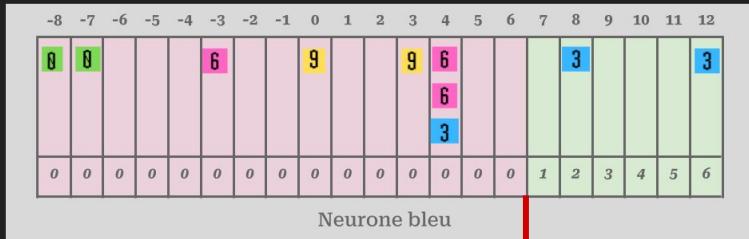




Neurone bleu



Neurone jaune



3	4	5	6	7	8	9	10	11	12	13	14	15
0	0	0	0	0	0	0	1	2	3	4	5	6
0	0	0	0	0	0	0	0	3	3	3	4	7

Neurone A

3	4	5	6	7	8	9	10	11	12	13	14	15
0	0	0	0	0	0	1	2	3	4	5	6	8
0	0	0	0	0	0	0	0	3	6	6	3	8

Neurone D

1	2	3	4	5	6	7	8	9	10	11	12	13
0	0	0	0	0	0	0	1	2	3	4	5	6
0	0	0	0	0	0	0	0	3	3	6	9	3

Neurone B

12	13	14	15	16	17	18	19	20	21	22	23	24
0	0	0	0	0	0	1	2	3	4	5	6	8
0	0	0	0	0	0	0	0	3	9	6	0	6

Neurone E

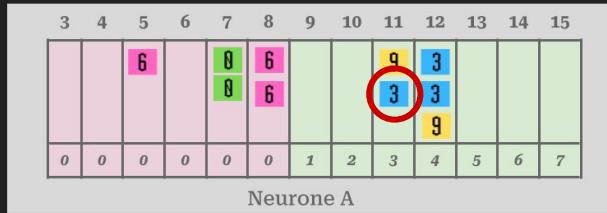
11	12	13	14	15	16	17	18	19	20	21	22	23
0	0	0	0	0	0	0	1	2	3	4	5	6
3				3	6	6		3	9	0	9	

Neurone C

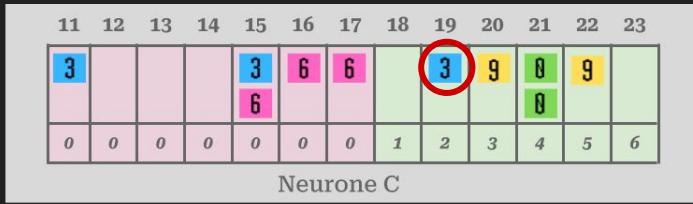
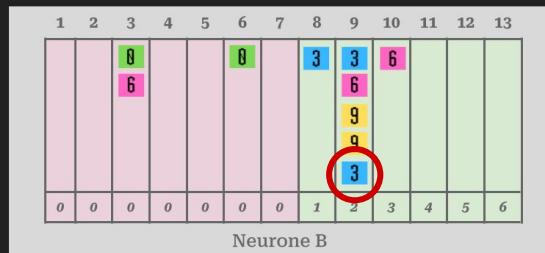
0	1	2	3	4	5	6	7	8	9	10	11	12
0	0	0	0	0	0	1	2	3	4	5	6	7
0	0	0	0	0	0	0	0	3	9	3	0	6

Neurone F

Neurone bleu : A + B + D - C - E

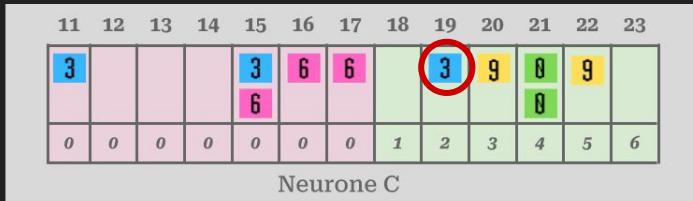
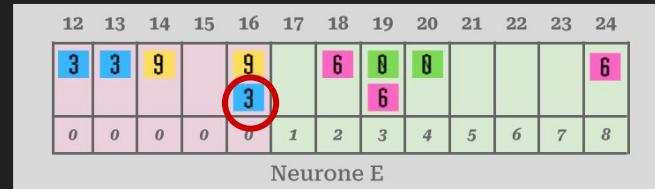
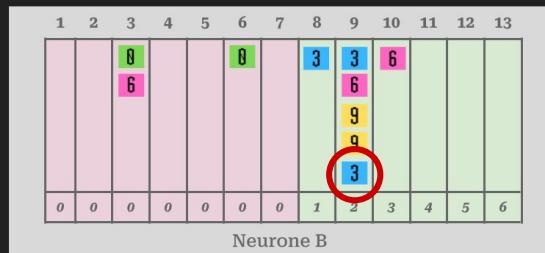
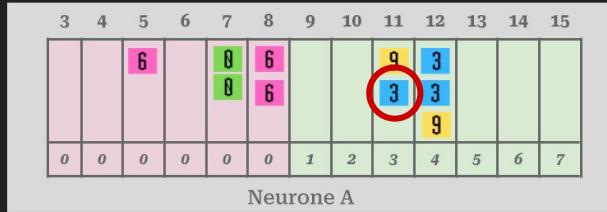


Neurone jaune : A + B + C - D - E



Neurone bleu : A + B + **D - C** - E

Neurone jaune : A + B + **C - D** - E



Neurone bleu : A + B + **D - C** - E

Neurone jaune : A + B + **C - D** - E

11	12	13	14	15	16	17	18	19	20	21	22	23
3				3	6	6		3	9	0	9	
0	0	0	0	0	0	0	1	2	3	4	5	6

Neurone C

3	4	5	6	7	8	9	10	11	12	13	14	15
		0	0		3		3		6	6		
0	0	0	0	0	1	2	3	4	5	6	7	8

Neurone D

Neurone bleu : A + B + **D - C** - E

Neurone jaune : A + B + **C - D** - E

11	12	13	14	15	16	17	18	19	20	21	22	23
3				3	6	6		3	9	0	9	
6				0	0	0	1	2	3	4	5	6

Neurone C

+1

11	12	13	14	15	16	17	18	19	20	21	22	23
3				3	6	6		3	9	0	9	
6				0	0	0	0	1	2	3	4	5

Neurone C

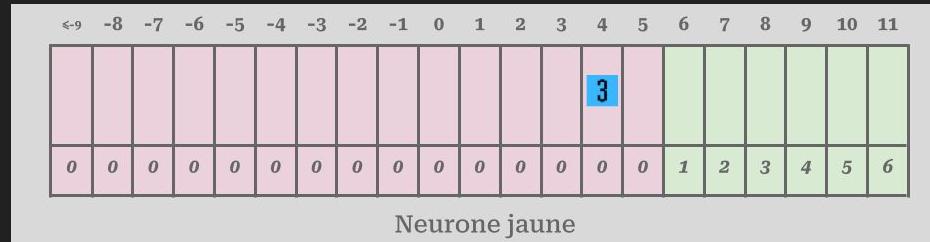
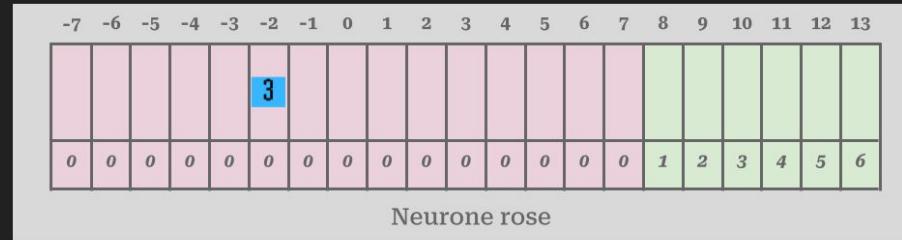
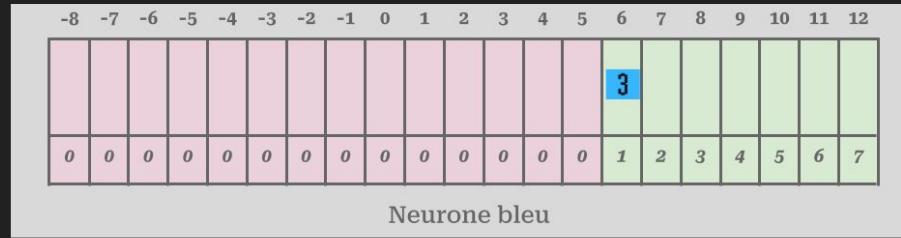
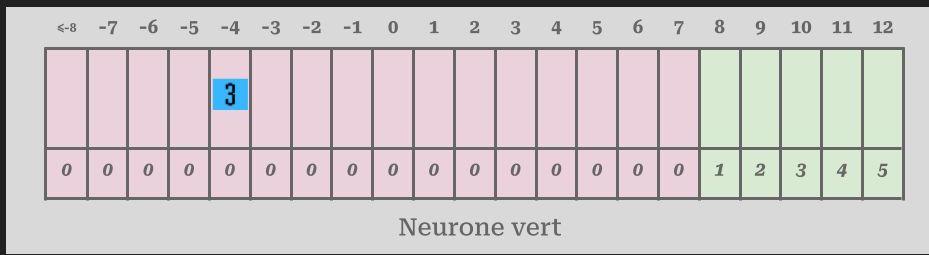
3	4	5	6	7	8	9	10	11	12	13	14	15
		0	0		3		3		6	6		
		9	9		0	0	0	1	2	3	4	5

Neurone D

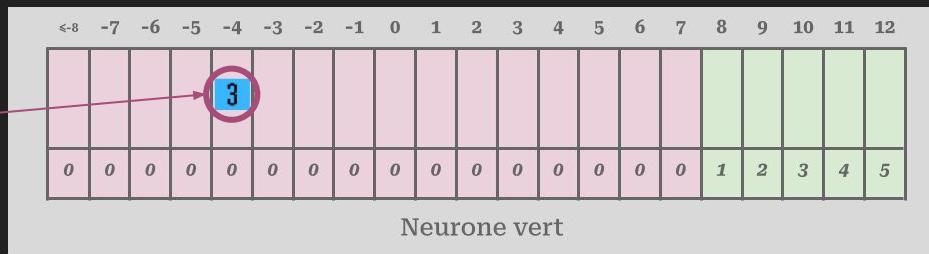
-1

3	4	5	6	7	8	9	10	11	12	13	14	15
		0	0		3		3		6	6		
		9	9		0	0	0	1	2	3	4	5

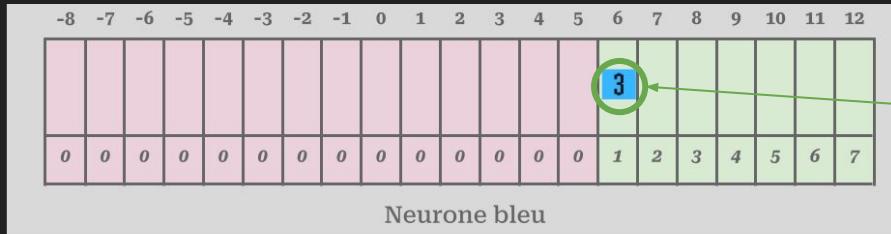
Neurone D



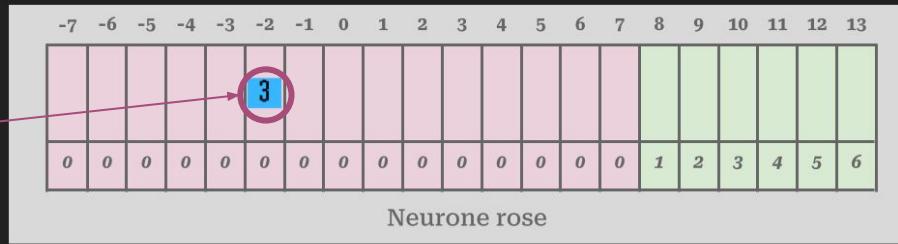
CE N'EST PAS UN 0



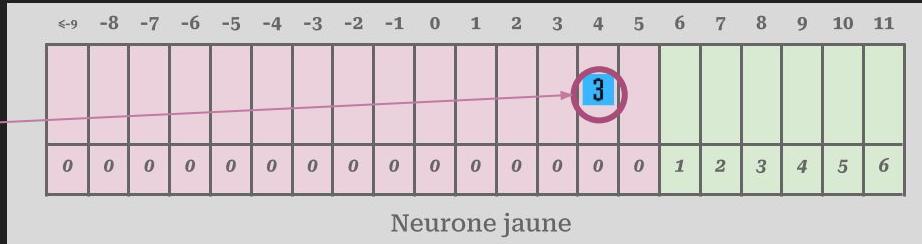
C'EST UN 3

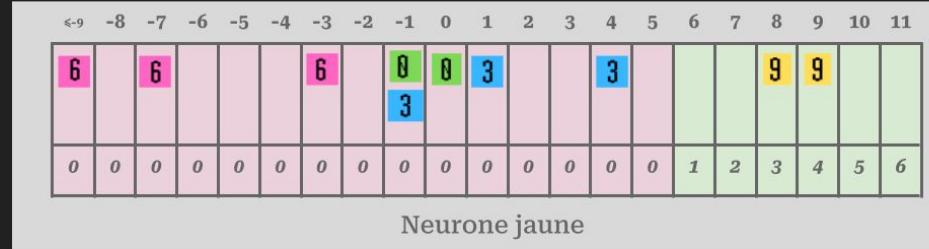
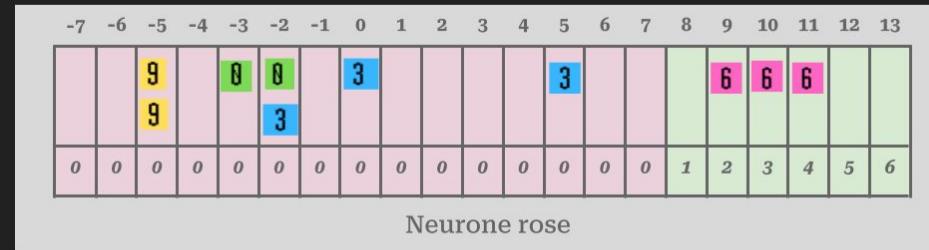
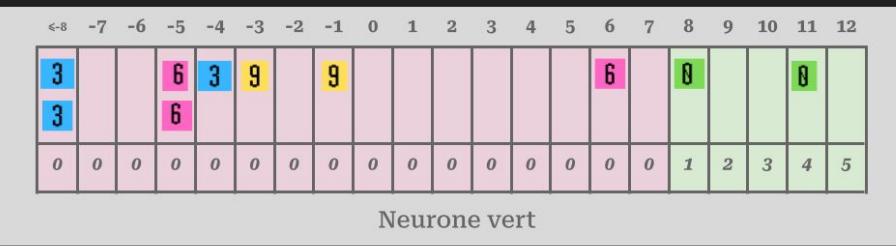


CE N'EST PAS UN 6

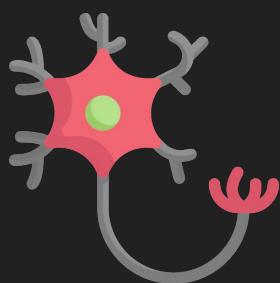


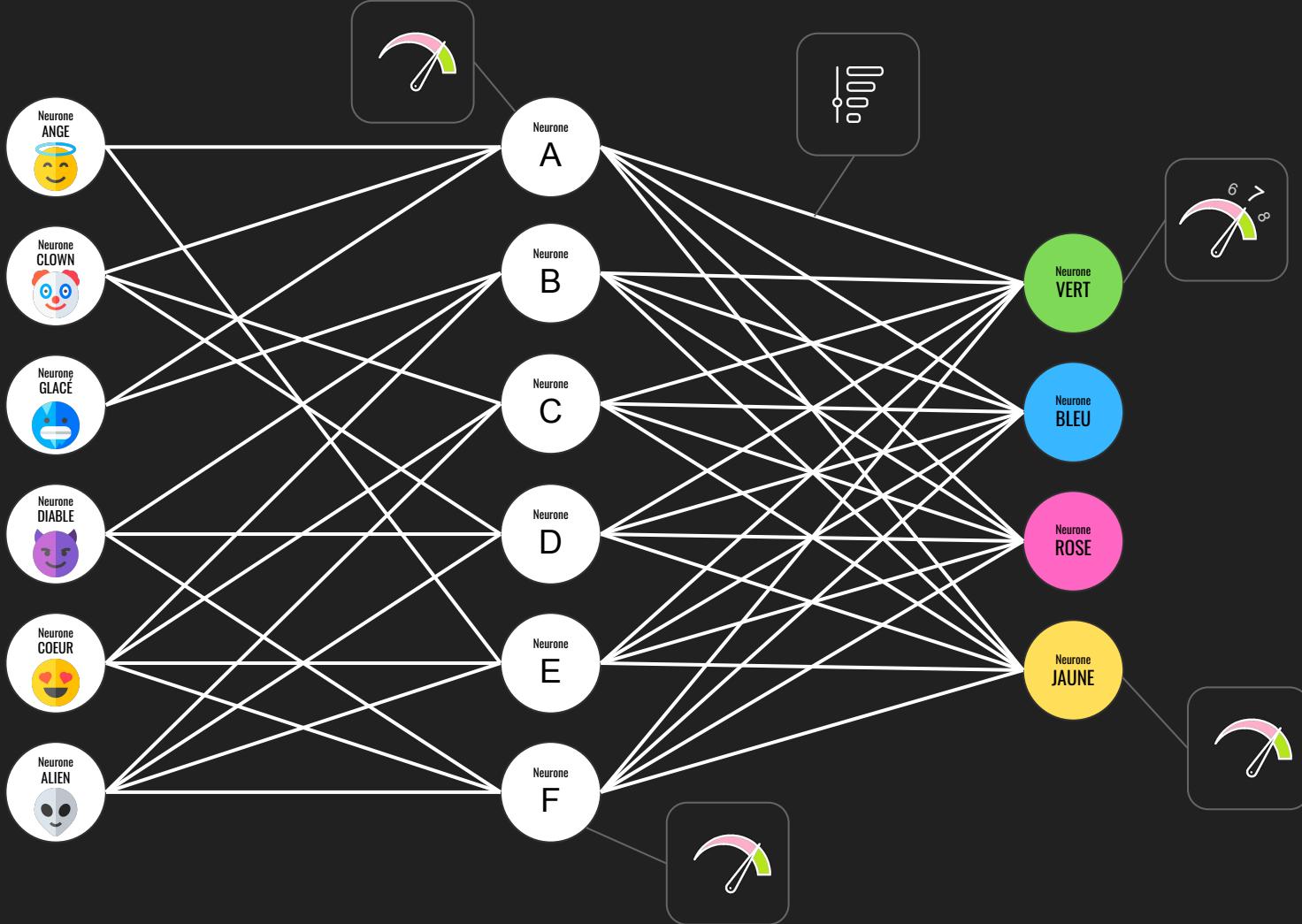
CE N'EST PAS UN 9





# Connecte tes neurones !





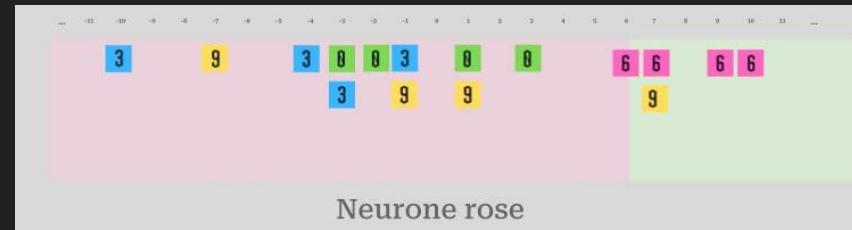
# Le réseau et son apprentissage en Python

# Le réseau et son apprentissage en Python

```
10 import numpy as np
11
12
13
14 sortie_cachée=np.empty((16,6),dtype='float64')
15 sortie_finale=np.empty((16,4),dtype='float64')
16 seuil_cache=np.empty((6,),dtype='float64')
17 seuil_final=np.empty((4,),dtypes='float64')
18 erreur=np.empty((16,6),dtype='float64')
19
20 ##### INITIALISATION DES POIDS ET DES SEUILS #####
21
22 W=np.empty((6,6),dtype='float64')
23 W[0]=[-1,1,1,0,0,0]
24 W[1]=[1,1,0,0,-1]
25 W[2]=[0,0,1,1,1,0]
26 W[3]=[0,1,0,-1,0,1]
27 W[4]=[1,0,0,0,1,1]
28 W[5]=[0,0,0,1,-1,1]
29
30 masque=np.empty((6,6))
31
32 masque[0]=[1,1,1,0,0,0]
33 masque[1]=[1,1,0,0,0,1]
34 masque[2]=[0,0,1,1,1,0]
35 masque[3]=[0,1,0,1,0,1]
36 masque[4]=[1,0,0,0,1,1]
37 masque[5]=[0,0,0,1,1,1]
38
39 seuil_cache=np.array([8,7,18,6,16,5],dtype='float64')
40
41 P=np.empty((4,6),dtype='float64')
42 P[0]=[-1,-1,-1,1,1]
43 P[1]=[1,1,-1,1,-1,0]
44 P[2]=[-1,1,-1,1,1,-1]
45 P[3]=[1,1,1,-1,-1,0]
46
47 seuil_final=np.array([7,5,6,5],dtype='float64')
48
49 ##### LES DONNÉES #####
50
51 test=np.empty((16,6),dtype='float64')
52
53 test[0]=[7,7,7,8,6,7]
54 test[1]=[6,4,9,6,6,7]
55 test[2]=[7,4,7,6,6,6]
56 test[3]=[4,5,8,5,7,5]
57 test[4]=[2,9,5,5,5,6]
58 test[5]=[1,10,3,3,5,6]
59 test[6]=[4,9,6,7,6,6]
60 test[7]=[2,8,8,7,5,6]
61 test[8]=[5,9,4,5,7,6]
62 test[9]=[5,9,4,4,7,7]
63 test[10]=[8,7,6,5,6,10]
64 test[11]=[4,9,6,4,8,7]
65 test[12]=[3,8,7,7,6,5]
66 test[13]=[4,7,8,7,7,5]
67 test[14]=[4,7,7,5,6,7]
68 test[15]=[5,6,7,6,7,5]
69
70 label = np.array([0,0,0,0,1,1,1,2,2,2,2,3,3,3,3])
```

```
73 ###### PARAMETRES DE L'APPRENTISSAGE #####
74
75
76 pas = 0.0001 #le pas dans le flot gradient
77 coef = 0.7 #coef dans la fonction de coût d'erreur qui est une fonction exponentielle
78
79 ##### L'APPRENTISSAGE PAR RETROPROPAGATION DU GRADIENT #####
80
81 # fonction de coût
82 def cout(y,l,a):
83     s = np.where(np.arange(4)[np.newaxis,:,:]==l[:,np.newaxis],-1,1)
84     return np.exp(a*s*y)
85
86 # dérivée de la fonction de coût
87 def dercout(y,l,a):
88     s = np.where(np.arange(4)[np.newaxis,:,:]==l[:,np.newaxis],-1,1)
89     return a*s*np.exp(a*s*y)
90
91 for epoche in range(100001):
92     #####calcul des sorties (passage forward)
93     # calcul de l'activité de la couche cachée par produit scalaire
94     # (i.e. somme pondérée) avec les entrées et ...
95     sortie_cachée = np.dot(test,W.T)-seuil_cache
96     # ... passage par la fonction d'activation ReLU
97     sortie_cachée = np.maximum(0,sortie_cachée)
98     # calcul de la sortie du réseau par produit scalaire avec la couche cachée
99     sortie_finale = np.dot(sortie_cachée,P.T)-seuil_final
100    # calcul de l'erreur du réseau
101    erreur = cout(sortie_finale,label,coef)
102    ##### fin du calcul des sorties #####
103    ##### ajustement des seuils et des poids #####
104    ##### ajustement des seuils finaux #####
105    # gradient de la couche de sortie
106    grad = dercout(sortie_finale,label,coef)
107    # mise à jour du seuil de la couche de sortie
108    seuil_final += 10*pas*np.sum(grad, axis=0)
109    # mise à jour des poids de la couche de sortie
110    P -= pas*np.dot(grad.T,sortie_cachée)
111    # rétropropagation du gradient à la couche cachée
112    grad_cache = np.dot(grad,P)*(sortie_cachée!=0) #sortie_cachée!=0 (dérivée de ReLU)
113    # mise à jour du seuil de la couche cachée
114    seuil_cache += pas*np.sum(grad_cache, axis=0)
115    # mise à jour des poids de la couche cachée
116    W -= pas*np.dot(grad_cache.T,test)
117    W *= masque # on force les connexions inexistantes à 0
118
119
120    #####calcul des sorties au final (passage forward)
121    sortie_cachée = np.dot(test,W.T)-seuil_cache[np.newaxis,:]
122    sortie_cachée = np.maximum(0,sortie_cachée)
123    sortie_finale = np.dot(sortie_cachée,P.T)-seuil_final[np.newaxis,:]
124    erreur = cout(sortie_finale,label,coef)
```

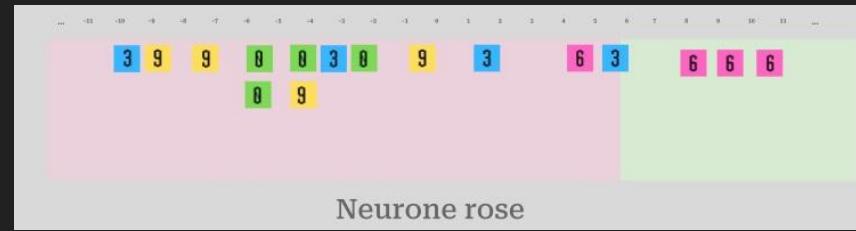
# Avec quelques exemples en plus



# Après 100 itérations



Neurone vert



Neurone rose

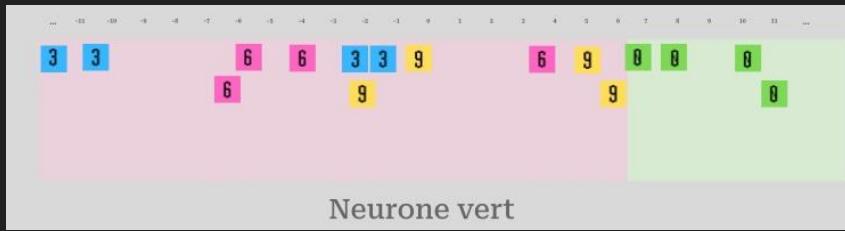


Neurone bleu

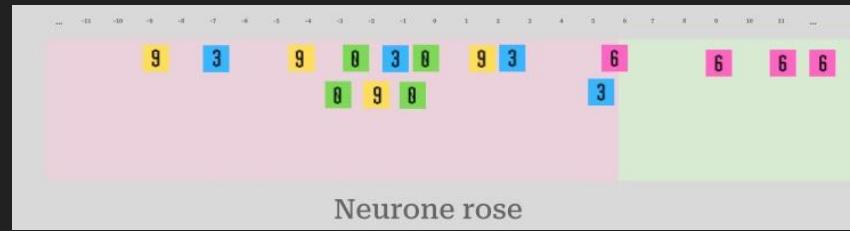


Neurone jaune

# Après 1000 itérations



Neurone vert



Neurone rose



Neurone bleu



Neurone jaune

# Après 5000 itérations



Neurone vert



Neurone rose

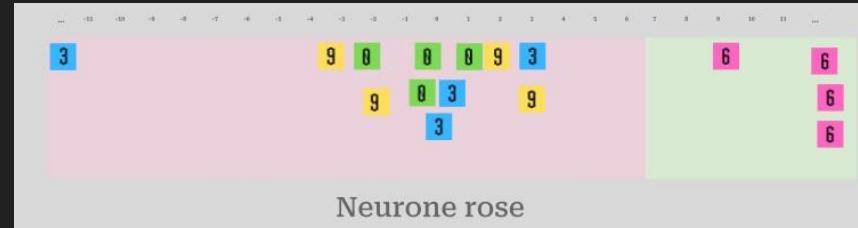


Neurone bleu

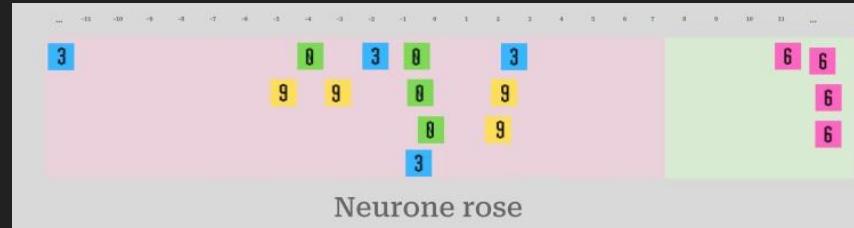


Neurone jaune

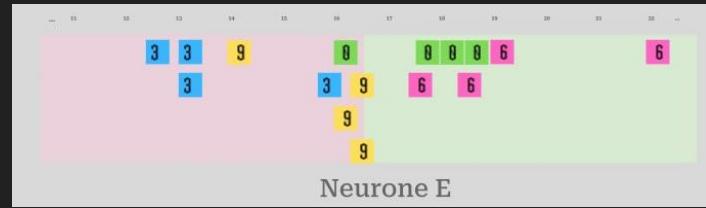
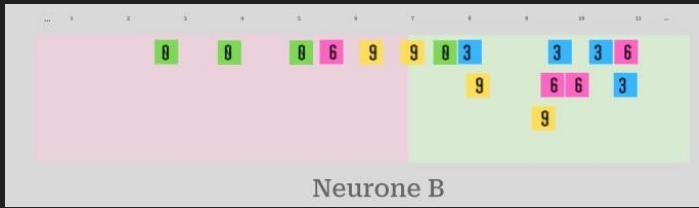
# Après 20000 itérations



# Après 50000 itérations



# Après 50000 itérations



Neurone bleu

2 A + 1,2 B - 1,1 C + 0,5 D - 2,7 E + 3 F

Neurone E

0,7 😇 + 1,2 😍 + 👽